## MATH 8600 (FALL 2018) HOMEWORK 4

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Assigned 10/12/2018, due 10/22/2018 by 5pm in my office.

1. Prob 5.22, 5.23, 5.24, 6.4, 6.5, 6.6(b)

Note that for 6.4(b), please add one column of data: i = 4,  $t_i = 3.0$  and  $z_i = e^{\pi}$ . Also, some of you might have  $v(t) = x_1 + x_1 t$ , where the second  $x_1$  should be  $x_2$ .

2. Write a MATLAB QR code using modified Gram-Schmidt orthogonalization discussed in class. Calculate the number of floating point operations needed (assuming  $A \in \mathbb{R}^{n \times m}$  is fully dense), and test it on two matrices

A1 = rand(10000, 45);

and

A = fliplr(vander(linspace(-1,1,10000))); A2 = A(:,1:25); A3 = A(:,1:45);

Check the 2-condition number of  $A_i$ ,  $||Q^TQ - I||_2$  and  $||QR - A_i||_2/||A_i||_2$ , for each of the three matrices, respectively. Draw conclusions from the numerical results.