

## MATH 8600 (FALL 2018) HOMEWORK 2

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Assigned 09/13/18, due 09/21/18 by 5pm in my office.

1. Textbook **Probs 3.1. 3.3. 3.4. 3.5. 3.7. 3.17.**
2. For a nonlinear system  $F(x) = 0$  ( $x \in \mathbb{R}^n$ ), let  $x^*$  be a solution, assume that  $J_F(x^*)$  is nonsingular, and that all the Hessians  $H_\ell = [\frac{\partial^2 f_\ell}{\partial x_i \partial x_j}]$  ( $1 \leq \ell \leq n$ ) are finite near  $x^*$ . Show that Newton's method

$$x^{(k+1)} = x^{(k)} - \left[ J_F(x^{(k)}) \right]^{-1} F(x^{(k)})$$

converges quadratically if  $x^{(k)}$  is sufficiently close to  $x^*$ .

3. Solve the nonlinear system of equations by Newton's method

$$\begin{cases} x_2^2 \cos x_1 + x_1 \ln x_3 = \pi - 4 \\ \cot \frac{x_1}{4} + x_2 x_3^2 = 1 + 2e^2 \\ x_3 \sin x_1 + x_2 \ln x_3 = 2 \end{cases}$$

Let  $x^{(0)} = [3 \ 3 \ 3]^T$  and show the error  $e_k = \|x^{(k)} - x^*\|$  where  $x^* = [\pi \ 2 \ e]^T$ .

4. **Prob 9.7.**